An Adaptive Problem-Solving Solution to Large-Scale Scheduling Problems

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Abstract

Although the general class of most scheduling problems is NP-hard, in practice, domain-specific techniques frequently solve problems in much better than exponential time. Unfortunately, constructing special-purpose systems is a knowledge—intensive and time-consuming process that requires a deep understanding of the domain and problem-solving architecture. The goal of our work is to develop techniques to allow for automated learning of an effective domain-specific search strategy given a general problem solver with a flexible control architecture. in this approach, a learning system explores a space of possible heuristic methods for one well-suited to the eccentricities of the, given domain and problem distribution. We discuss an application of the approach to scheduling satellite communications. Using problem distributions based on actual mission requirements, our approach identifies strategies that not only decrease the amount of CPU time required to produce schedules, but also increase the percentage of problems that are solvable within computational resource limitations.

Keywords

scheduling, machine learning, adaptive problem solving, utility problem

1 INTRODUCTION

With the maturation of automated problem-solving research has come grudging abandonment of the search for "the" domain-independent problem solver. Genera] problem-solving tasks like planning and scheduling are provably intractable. Although heuristic methods are effective in many practical situations, an ever growing body of work demonstrates the narrowness of specific heuristic strategies (e.g., [Baker94, Frost94, Kambhampati95, Stone94, Yang94]). Studies repeatedly show that a strategy that excels on one task can perform abysmal 1y on others. These negative results do not entirely discredit domain-independent approaches, but they suggests that considerable effort and expertise is required to find an accept able combination of heuristic methods. 1 n fact, the few published accounts of real-world implementations lend support to this conjecture (e.g. [Wilkins88]). The specificity of heuristic methods is especially troubling when we consider that problem-solving tasks frequently change over time. Thus, a heuristic problem solver may require expensive "tune-ups" as the character character of the application changes.

Adaptive problem solving is a general method for reducing the cost of developing and maintaining effective heuristic problem solvers. Rather than forcing a developer to choose a specific heuristic strategy, an adaptive problem solver adjusts itself to the idiosyncrasies of an application. This can be seen as a natural extension of the principle of least commitment [Sacerdoti77]. When solving a problem, one should not commit to a particular solution path until one has information to distinguishes that path from the alternatives. Likewise, when faced with an entire distribution of problems, it makes sense to avoid committing to a particular heuristic strategy until one can make an informed decision on which strategy performs better on the distribution. An adaptive problem solver embodies a space of heuristic methods, and only settles on a particular combination of these methods after a period of adaptation, during which the system automatically acquires information about the particular distribution of problems associated with the intended application.

in previous art icles, the first author has presented a formal characterization of adaptive problem solving and has developed a general a general method for transforming a standard problem solver into an adaptive onc [Gratch92, Gratch94]. The primary purpose of this article is to build empirical support for the method by illustrating its application to a real-world problem solving task. After reviewing the basic method, we describe its application to the development of a large-scale scheduling system for the National Aeronautics and Space Administration (NASA). We applied the adaptive problem solving approach to a prototype scheduling system that was developed and by a separate research group, and without knowledge of our adaptive techniques. The prototype scheduler included an expert-crafted scheduling strategy to achieve efficient scheduling performance. By auto-

matically adapting this scheduling system to the distribution of scheduling problems, the adaptive approach resulted in a significant improvement inscheduling performance over an already optimized strategy: the best adaptation found by machine learning exhibited an seventy percent improvement in scheduling performance. The article is organized as follows: the next section (Section 2) motivates the need for adaptive problem solving and provides a formal definition of the task; Section 3 reviews the COMPOSER system (a general approach for constructing an adaptive problem solver); Section 4 describes the scheduling task, which involves scheduling communication events between earth-orbiting satellites and fixed ground stations; Section 5 details how we applied adaptive problem solving to efficiently construct an effective solution to this complex scheduling problem; Section 6 reports on a series of empirical evaluations of the adaptive scheduling system; Section 7 discusses future work and Section 8 summarizes this article's contributions.

2 ADAPTIVE PROBLEM SOLVING

An adaptive problem solver defers the selection of a heuristic strategy until some information can be gathered about their performance over the specific distribution of tasks. The need for such an approach is predicated on the claim that it is difficult to identify an effective heuristic strategy *a prio-ri*. While this claim is by no means proven, there is considerable evidence that, at least for the class of heuristics that have been proposed till now, no one collection of heuristic methods will suffice. For example, Kambhampati, Knoblock, and Yang [Kambhampati95] illustrate how planning heuristics embody *designtradeoffs*—heuristics that reduce the size of search space typically increase the cost at each node, and vice versa—and that the desired tradeoff varies with different domains. Similar observations have been made in the context of constraint satisfaction problems [Baker94, Frost94]. This inherent difficulty in recognizing the worth (or lack of worth) of control knowledge has been termed the *utility problem*[Minton88] and has been studied extensively in the machine learning community [Gratch92, Greiner92, Holder92, Subramanian92]. In our case the utility problem is determining the worth of a heuristic strategy for specific problem distribution.

2.1 FO1<M1II.ATION OF ADAPTIVE PROBLEM SOLVING

Before discussing approaches to adaptive problem solving, we formally state the common definition of the task (see [Gratch92, Greiner92, Laird92, Subramanian92]). Adaptive problem solving requires a flexible problem solver, meaning the problem solver possesses control decisions that may be resolved in alternative ways. Given a flexible problem solver, PS, with several control points, CP_n (where each control point CP_i corresponds to a particular control decision), and a set of

alternative heuristic methods for each control point, $\{M_{i,1}...M_{i,k}, \}$,] a control strategy defines a specific method for every control point (c. g, $SHUT = \langle M_{1,3}, M_{2,6}, M_{3,1},... \rangle$). A control strategy determines the overal I behavior oft he problem solver. Let PS_{STRAT} be the problem solver operating under a particular control strategy.

The quality of a problem solving strategy is defined in terms of the decision-theoretic notion of expected utility. Let $U(PS_{STRAT}; d)$, is a real valued *utility function* that is a measure of the goodness of the behavior of the problem solver over problem d. Expected utility is defined formally as:

$$E_D[U(PS_{STRAT})] = \sum_{d \in D} U(PS_{STRAT}, d)^x probability(d)$$

The goal of adaptive problem solving can be expressed as: given a problem distribution D, find some control strategy in the space of possible strategies that maximizes the expected utility of the problem solver. For example, in the PRODIGY planning system [Minton88], control points include: how to select an operator to use to achieve the goal; how to select variable bindings to instantiate the operator; etc. A method for the operator choice cent rol point might be a set of control rules to determine which operat ors to use to achieve various goals. A strategy for PRODIG Y would be a set of control rules and default methods for every control point (e.g., one for operator choice, one for binding choice, etc.). Utility might be defined as a function of the time to construct a plan for a given planning problem.

2.2 APPROACHES TO ADAPTIVE PROBLEM SOLVING

Three potentially complementary approaches to adaptive problem solving have been discussed in the literature. The first, what we call a *syntactic approach*, *is* to preprocess a problem-solving domain into a more efficient form, based solely on the domain's syntactic structure. For example, Etzioni's STATIC system analyzes a portion of a planing domain's deductive closure to conjecture a set of search control heuristics [Etzioni90]. Dechter and Pear] describe a class of constraint satisfaction techniques that preprocess a general class of problems into a more efficient form [Dechter87]. More recent work has focused on recognizing those structural properties that influence the effectiveness of different heuristic methods [Frost94, Kambhampat i95, Stone94]. The goal of this research is to provide a problem solver with what is essentially a big lookup table, specifying which heuristic strategy to use based on some easily recognizable syntactic features of a domain, While this later approach seems promising, work in this area is still preliminary and has focused primarily on artificial applications. The disadvantage of purely syntactic techniques is that that they ignore a potentially important source of information, the distribution of problems. Furthermore, current syntactic ap-

^{1.} Note that a method may consist of smaller elements so that a method may be a set of control rules or a combination of heuristics.

proaches to this problem have not been very genera]: they typically apply to a narrow class of problems and arc specific to a particular, often unarticulated, utility function (usually problem-solving cost),

The second approach, which we call a *generative approach*, is to generate custom-made heuristics in response to careful, automatic, analysis of past problem-solving attempts. Generative approaches consider not only the structure of the domain, but also structures that arise from the problem solver interacting with specific problems from the domain. This approach is exemplified by SOAR [Laird86] and the PRODIGY/EBL system of Steve Minton [Minton88]. These techniques analyze past problem-solving traces and conjectures heuristic control rules in response to specific problem-solving inefficiencies. Such approaches can effectively exploit the idiosyncratic structure of a domain through this careful analysis. The limitation of such approaches is that they have typically focused on generating heuristics in response to particular problems and have not well addressed the issue of adapting to a distribution of problems. Furthermore, as with the syntactic approaches, thus far they have been directed towards a specific utility function,

The final approach we call the *statistical approach*. These techniques explicit] y reason about performance of different heuristic strategies across the distribution of problems. These are generally statistical gcl~cr:ltc-:tn(l-test approaches that cst i mated the average performance of different heuristics from a random set oft raining examples, and explore an explicit space of heuristics with greedy search techniques. Examples of such systems are. the COMPOSER system of Gratch and DcJong [Gratch92], the PALO system of Grcincr and Jurisica[Grciner92], and the statistical component of Minton's MULTI-TAC[Minton93]. Similar approaches have also been investigated in the operations research community [Yakowitz90]. These techniques are easy to usc, apply to a variety of domains and utility functions, and can provide strong statistical guarantees about their performance. They are limited, however, as they are computationally expensive, require many training examples to identify a strategy, and face problems with local maxima. Furthermore, they typically leave it to the user to conjecture the space of heuristic methods (scc[Minton93] for a notable exception).

In this article, we adopt the statistical approach to adaptive problem solving due to its generality and case of USC. in particular we use the COMPOSER technique for adaptive problem solving [Gratch92, Gratch94], which is reviewed in the next section. Our implementation incorporates some novel features to address the computational expense of the method. Ideally, however, an adaptive problem solver would incorporate some form of each of these methods, To this end we are investigating how to incorporate other methods of adaptation in our current research.

3 COMPOSER

COMPOSER embodies a statistical approach to adaptive problem solving. To turn a problem solver into an adaptive problem solver, the developer is required to specify a utility function, a representative sample of training problems, and a space of possible heuristic strategies. COMPOSER then adapts the problem solver by exploring the space of heuristics via statistical hillclimbing search. The *search* space is defined in terms of a *transformation generator* which takes a strategy and generates a set of transformations to it. For example, one simple transformation generator just returns all single method modifications to a given strategy. Thus a transformation generator defines both a space of possible heuristic strategies and the non-deterministic order in which Ibis space maybe searched. COMPOSER'S overall approach is one of generate and test hillclimbing. Given an initial problem solver, the transformation generator returns a set of possible transformations to its control strategy. These are statistically evaluated over the expected distribution of problems. A transformation is adopted if it increases the expected performance of solving problems over that distribution. The generater then constructs a set oft ransformat ions to this new strategy and so on, climbing the gradient of expected utility values.

Formally, COMPOSER t akes an initial problem solver, PSo, and identifies a sequence of problem solvers, PS_0, PS_1, \ldots where each subsequent PS has higher expected utility with probability $1 - \delta$ (where $\delta > 0$ is some user-specified constant). The transformation generator, TG, is a function that t akes a problem solver and returns a set of candidate changes. Apply(t, PS) is a function that takes a transformation, $t \in TG(PS)$ and a problem solver and returns a new problem solver t hat is the result of transforming PS with t.1 $\cot U_i(PS)$ denote the utility of PS on problem j. The change in utility that a transformation provides for the jth problem, called the incremental utility of a transformation, is denoted by $\Delta U_i(t|PS)$. This is the difference in utility between solving the problem with and without the transformation. COMPOSER finds a problem solver with high expected utility by identifying transformations with positive expected incremental utility. The expected incremental utility is estimated by averaging a sample of randomly drawn incremental utility values. Given a sample of *n* values, the average of that sample is denoted by $\overline{\Delta U}_n(t|PS)$. The likely difference between the average and the true expected incremental utility depends on the variance of the distribution, estimated from a sample by the sample variance $S_n^2(t|PS)$, and the size of the sample, n. COMPOSER provides a statistical technique for determining when sufficient examples have been gathered to decide, with error δ , that the expected incremental utility of a transformation is positive or negative. The algorithm is summarized in Figure 1.

```
Given: PS_{old}, TG(\cdot), \delta, examples
[1] PS := PS_{old}; 7' := TG(PS); i := O; n := O; \alpha := Bound(\delta, 171);
                                                                     /* 1 lillclimb as long as there is data and possible transformations */
[2] While T \neq 0 and n < lexamples do
                             /* Findnexttransformation*/
[3]
            Repeal
[4]
                   i := i+1; n := n+1; step-taken := FALSE;
                   \forall \tau \in '1' : \operatorname{Get} \Delta U_i(\tau | PS)
[5]
                                                                      /* Observe incremental utility values for ith problem */
                   significant := \begin{cases} \tau \in 7': \ n \ge n_0 \ \text{ and } \frac{C^2 \mathcal{G}_n^* \{P, S_L\}}{\left[ \overline{\Delta U}_n(\tau | PS) \right]^{-2}} < \frac{n}{2} < \frac{n}{2} / \text{* Collect all transformations */} \\ \left[ \overline{Q(\alpha)} \right]_1^2 / \text{* statistical significance. * /} \end{cases}
[6]
                    T:=T-\{\tau\in significant: \Delta U_n(\tau|PS)<\mathbf{0}\} /* Discard trans. that decrease expected utility */
[7]
                   If \exists \tau \in significant : \overline{4} \dot{U}_n(\tau | PS) > \mathbf{0} Then /* Adopt \tau that most increases expected utility */
[8]
[9]
                          PS = Apply(x \in significant : \forall y \in significant \left[ \Delta U_n(x|PS) > \Delta \overline{U}_n(y|PS) \right], PS
[10]
                          7' := TG(PS); n := o; \alpha := Bound(\delta, |T|); step--taken := TRUE;
[11]
            Until step-taken or T=\emptyset or n=lexamplesl;
```

Return: PS $Bound(\delta, |T|) := \frac{\delta}{|T|}, \qquad Q(\alpha) := x \text{ where } \int_{y}^{\infty} 1_{(1/\sqrt{2\pi})} e^{-0.5y^2} dy = \frac{\alpha}{2}$

Figure 1: The COMPOSER algorithm

COMPOSER'S technique is applicable in cases where the following conditions apply:

- 1. The control strategy space can be structured to facilitate hillclimbing search. In general, the space of such strategies is so large as to make exhaustive search intractable. COMPOSER requires a transformation generator that structures this space into a sequence of search steps, with relatively few transformations at each step. in Section 5.1 we discuss some techniques for incorporating domain specific information into the structuring of the control strategy space.
- 2. There is a large supply of representative training problems so that an adequate sampling of problems can be used to estimate expected utility for various control strategies.
- 3. Problems can be solved with a sufficiently low cost in resources so that estimating expected utility is feasible.
- 4. There is sufficient regularity in the domain such that the cost of learning a good strategy can be amortized over the gains in solving many problems.

4 THE DEEP SPACE NETWORK

The Deep Space Network (DSN) is a multi-national collection of ground-based radio antennas responsible for maintaining communications with research satellites and deep space probes. DSN Operations is responsible for scheduling communicant i ons for a large and growing number of spacecraft. This already complex scheduling problem is becoming more challenging each year as budgetary pressures limit the construction of new antennas. As a result, DSN Operations has turned increasingly towards intelligent scheduling techniques as a way of increasing the efficiency of network utilization. As part of this ongoing effort, the Jet Propulsion Laboratory (JPL) has been given the responsibility of automating the scheduling of the 26-meter sub-net; a collection of three 26-meter antennas at Goldstone, CA, Canberra, Australia and Madrid, Spain.

in this section we discuss the application of adaptive problem-solving techniques to the development of a prototype system for automated scheduling of the 26-meter sub-net. We first discuss the development of the basic scheduling system and then discuss how adaptive problem solving enhanced the scheduler's effectiveness.

4.1 THE SCHEDULING PROBLEM

Scheduling the DSN 26-meter subnet can be viewed as a large constraint satisfaction problem. Each satellite has a set of constraints, called project requirements, that define its communication needs. A typical project specifics three generic requirements: the minimum and maximum number of communication events required in a fixed period of time; the minimum and maximum duration for these communication events; and the minimum and maximum allowable gap between communication events. For example, Nimbus-7, a meteorological satellite, must have at least four 1 S-minute communication slots per day, and these slots cannot be greater than five hours apart. Project requirements are determined by the project managers and tend to be invariant across the lifetime of the spacecraft.

In addition to project requirements, there are constraints associated with the various antennas. First, antennas are a limited resource – two satellites cannot communicate with a given antenna at the same time. Second, a satellite can only communicate with a given antenna at certain times, depending on when its orbit brings it within view of the antenna. Finally, antennas undergo routine maintenance and cannot communicate with any satellite during these times.

Scheduling is done on a weekly basis. A weekly scheduling problem is defined by three elements: (1) the set of satellites to be scheduled, (2) the constraints associated with each satellite, and (3) a set of *time periods* specifying all temporal intervals when a satellite can legally communicate with an antenna for that week. Each time period is a tuple specifying a satellite, a communication time

interval, and an antenna, where (1) the time interval must satisfy the communication duration constraints for the satellite, (2) the satellite must be in view of the antenna during this interval. Antenna maintenance is treated as a project with time periods and constraints. Two time periods conflict if they use the same antenna and overlap in temporal extent. A valid schedule specifies a non-conflicting subset of all possible time periods where each project's requirements are satisfied.

The automated scheduler must generate schedules quickly as scheduling problems are frequently over-constrained (i.e. the project constraints combined with the allowable views produces a set of constrains which is unsatisfiable) When this occurs, DSN Operations must go through a complex cycle of negotiating with project managers to reduce their requirements. A goal of automated scheduling is to provide a system with relatively quick response time so that a human user may interact with the scheduler and perform "what if" reasoning to assist in this negotiation process. Ultimately, the goal is to automate this negotiation process as well, which will place even greater demands on scheduler response t i me (see [Chien94] for some preliminary work on th is 1 ater problem). For these reasons, the focus of development is upon heuristic techniques that do not necessarily uncover the optimal schedule, but rather produce a adequate schedule quickly.

4.2 THE LR-26 SCHEDULER

1X-26 is a heuristic scheduling approach to DSN scheduling being developed at the Jet Propulsion Laboratory [Bell93]. 2 1X-26 is based on a O-1 integer linear programming formulation of the problem [Taha82]. Scheduling is cast as the problem of finding an assignment to integer variables that maximizes the value of some *objective function* subject to a set of linear constraints. In particular, time periods are treated as O-1 integer variables: O (or OUT) if the time period is excluded from the schedule; 1 (or IN) if it is included. The objective is to maximize the number of time periods in the schedule and the solution must satisfy the project requirements and antenna constraints (expressed as sets of linear inequalities). A t ypical scheduling problem under this formulation has 700 variables and 1300 constraints.

In operations research, integer programs are solved by a variety of techniques including branch-and-bound search, the gomory method [Kwak87], and Lagrangian relaxation [I~ishcr81]. In artificial intelligence such problems are solved by constraint propagation search techniques such as [Dechter92, Mackworth92]. To address the complexity of the scheduling problem 1.1<-26 uses a hybrid approach that combines Lagrangian relaxation with constraint propagation search. Lagrangian relaxation is a divide-and-conquer method which, given a decomposition of the scheduling problem into a set of easier sub-problems, coerces the sub-problems to be solved in such a way that they frequently result

^{2. 1}X-26 stands for the Lagrangian Relaxation approach to scheduling the 26-meter sub-net (see below).

in a global solution. One specifies a problem decomposition by identifying a subset of problem constraints that, if removed, result in one or more independent and computationally easy sub-problems.³ These problematic constraints are "relaxed," meaning they no longer act as constraints but instead are added to the objective function in such that way that (1) there is incentive to satisfying these relaxed constraints when solving the sub-problems and, (2) the best solution to the relaxed problem, if it satisfies all relaxed constraints, is guaranteed to be the. best solution to the original problem. Furthermore, this relaxed objective function is parameterized by a set of weights (one for each relaxed constraint). By systematically changing these weights (thereby modifying the relaxed objective function) the sub-problems can often be coerced into producing a global solution. Even if this weight search dots not produce a global solution, it can make the solution to the sub-problems sufficiently close to a global solution that a global solution can be discovered with substantially reduced constraint propagation search.

In the DSN domain, the scheduling problem is decomposed by scheduling each antenna independently. Specifically, the constraints associated with the complete problem can be divided into two groups: those that refer to a single antenna, and those that mention multiple antennas. The later are relaxed and the resulting single-antenna sub-problems can be solved in time linear in the number of time periods associated with that antenna (see below). LR-26 solves the complete problem by first trying to coerce a global solution by performing a search in the space of weights and then, if that fails to produce a solution, resorting to constraint propagation search in the space of possible schedules.

4.2.1 Variables and Schedules

We now describe the formalization of the problem. Let P be a set of projects, A a set of antennas, and $M = \{O,..., 10080\}$ be the minutes in a week. Let $V \subseteq P \times A \times M \times M$ denote the set of possible time periods for a week, where a given time period specifies a project, antenna and the start and end of the communication event, respectively. For a given $v_i \in V$, let $project(v_i)$, $antenna(v_i)$, $start(v_i)$, and $end(v_i)$ denote the corresponding elements of v_i .

With each time period, $v_i \cdot V$, we associate a O--1 integer variable, which we will refer to as vi for compact ness. Let $v_i = 1$ ($v_i = IN$) mean that the time period is included in the schedule and $v_i = O$ ($v_i = OUT$) mean that the time period is excluded from the schedule. A ground schedule is an assignment of zero or one to each $v_i \in V$. We can denote a ground schedule by an variable assignment function $s: V \rightarrow \{O, 1\}$. A partial schedule refers to a schedule with only a subset of its variables assigned a value, denoted by a partial assignment function $s_p: V \rightarrow \{0, 1, ?\}$ (where "?" indicates that the vari-

3. A problem consists of *independent* sub-problems it the global objective function can be maximized by finding some maximal solution for each sub-problem in isolation.

able could be either in or out of the ground schedule). A partial schedule corresponds a set of ground schedules consistent with the partial assignment. The completely uncommitted partial schedule (with no variables assigned a value), $s_0: V \rightarrow \{?\}$, denotes the set of all possible ground schedules,

4.2.2 Constraints

Each project $p_j \in P$ associated with a set of constraints called project requirements. All constraints are processed and translated into simple linear inequalities over elements of V. Project requirements can be partitioned into two sets of linear inequalities based on their syntactic form:

$$R_I = \{ \Sigma_j \ a_{ij} \cdot v_j \ge b_i \}, \qquad R_2 = \{ \Sigma_j \ a_{ij} \cdot v_j \le b_i \}.$$

where a_{ij} represents a weighting factor indicating the degree to which a particular view contributes to satisfying a constraint. For example, the constraint that a project, p_j , must have at least 100 minutes of communication time in a week is a member of R_I :

$$\sum_{v_i \in Vproject(v_i) = p_j} v_i [end(v_i) - start(v_i)] \geq 100.$$

The constraint on the minimum and maximum duration for a communication event is satisfied implicitly in the definition of $V: vi \in Viff$ rein-duration $\leq end(v_i) - start(v_i) \leq \max$ -duration. All project requirements can be straightforwardly translated into a set on linear inequalities.

Each of the three antennas has the constraint that no two projects can use the antenna at the same time. This can be translated into a set of linear inequalities C_a for each antenna a as follows:

$$C_a = \{ v_i + v_i \le 1 | v_i # v_i \land antenna(v_i) = antenna(v_i) = a \land [start(v_i)..end(v_i)] \land [start(v_i)..end(v_i)] # \emptyset \}$$

4.2.3 Problem Formulation

The basic scheduling objective is find some ground schedule, denoted by s^* , that maximizes the number of time periods in the schedule subject to the project and antenna constraints:⁵

Problem: DSN

Find:
$$s^* = \arg \max_{s \in s_0} Z = \sum_{V} v_j$$
 (1)

Subject to: $c_1 \cup C_2 \cup C_3 \cup R_1 \cup R_2$

^{4.} This restriction is an inherent limitation in the formalization as the scheduler cannot entertain variable length communication events – communication events must be descretized into a finite set of fi xed length intervals.

^{5.} This might correspond to the desire to maintain maximum downlink flexibility. Alternative formalization might attempt to minimize the number of views in the schedule to model reducing operations costs.

With Lagrangian relaxation, only the antenna constraints are retained and the remaining constraints are folded into the objective function. The Lagrangian relaxation formulation of the problem (due to Colin Bell) is:

Problem: DSN(u)

Find:
$$s^*(u) = \arg \max_{s \in s_0} \left\{ Z(u) = \sum_{V} v_f - \sum_{R_1} u_i \left[\sum_{i} a_{ij} v_f - b_i \right] - \sum_{R_2} u_i \left[b_i - \sum_{i} a_{ij} v_j \right] \right\}$$
 (2)

Subject to: $c_1 \cup C_2 \cup C_3$

where Z(u) is the relaxed objective function and u is a vector of non-negative weights of length $|R_I \cup R_2|$ I (one for each relaxed constraint). Note that this defines a space of relaxed problems that depend on the weight vector u. Let Z^* denote the value of the optimal solution of the original problem (Definition 1), and let $Z^*(u)$ denote value of the optimal solution to the relaxed problem (Definition 2) for a particular weight vector u. For any weight vector u, $Z^*(u)$ can be shown to be an upper bound on the value of Z^* . Thus, if a relaxed solution satisfies all of the original problem constraints, it is guaranteed to be the optimal solution to the original problem (i.e. $s_u^* = s^*$). Lagrangian relaxation proceeds by incrementally tightening this upper bound (by adjusting the weight vector) in the hope of identifying a global solution. A global solution cannot always be identified in this manner, so a compete scheduler must combine Lagrangian relaxation with some for of search.

4.2.4 Search

The original problem formulation (1), can be solved (expensively!) by basic *refinement search* [Kambhampati95] (or split-and-prune search [Dechter87]) in the space of partial schedules. In this search paradigm a partial schedule is recursively refined (split) into a set of more specific partial schedules. In LR-26, refinement is clone by forcing uncommitted time periods in or out of the schedule. For example, a time period is excluded from the schedule if it temporally conflicts with a time period that has been forced in. Search continues non-deterministically until the best ground schedule is found or all schedules are pruned.

Each refinement is further refined by propagating the local consequence of new commitment. After a variable is set to a particular value, each individual constraint which references that variable is analyzed to determine which view would be forced in or out of the schedule as a result of the assignment. LR–26 performs only partial constraint propagation, because complete propagation is computationally expensive. Specifically, if constraint Cl references variables V₂, V₄ and V₅, and V₂ is assigned

a value, LR-26 analyzes C 1 to see if the new assignment determines the value of V_4 and/or V_5 . If, for example, V_4 is constrained to take on a particular value, this triggers analysis of all constraints which contain V_4 . This can be viewed as performing are-consistency [Dechter92]. During the constraint propagation it may be possible to show that the refinement contains no valid ground schedule. In this case the partial schedule may be pruned from the search.

LR-26 augments this basic refinement search with Lagrangian relaxation to heuristically reduce the combinatorics of the problem. The difficulty with refinement search is it may have to perform considerable (and poorly directed) search through a tree of refinements to identify a *single* satisficing solution. If an optima] solution is sought, every leaf of this search tree must be examined. ^bIn contrast, by searching through the space of relaxed solutions to a partial schedule, one can sometimes identify the *best* schedule without any refinement search. Even when this is not possible, Lagrangian relaxation heuristically identifies a small set of problematic constraints, focusing the subsequent refinement search. Thus, by performing some search in the space of relaxed solutions at each step, the augmented search method can significantly reduce both the depth and breadth of refinement search.

The augmented procedure works to the extent that it can efficiently solve relaxed solutions, ideally allowing the algorithm to explore several points in the space of weight vectors in each step of the refinement search. LR-26 solves relaxed problems in linear time, $O(|C_1 \cup C_2 \cup C_3|)$. To see this, note that each time period appears on exact 1 y one antenna. Thus Z(u) can be broken into the sum of three objective functions, each containing only the time periods associated with a particular antenna. Each of these single antenna problems can be formulated and solved as a problem of finding the longest path in an acyclic network: sort time periods by their start time; then for each view in sequence either (1) exclude the time period, leaving the value of the schedule unchanged, and proceed to next time period in sequence, or (2) include the time period, increasing the value of the schedule by an amount determined by the weight coefficients in the relaxed objective function, and proceed to next non-overlapping time period in sequence. This can be solved in linear time by dynamic programming (see [Bell93] for more details).

^{6.} Partial schedules may also be pruned, as in branch-and-bound search, if they can be shown to contain lower value solutions that other partial schedules. In practice I R-26 is run in a *satisficing mode*, meaning that search terminates as soon as a ground schedule is found (not necessarily optimal) that satisfies all of the problem constraints.

The augmented refinement search performed by I.R-26 is summarized as follows:

```
1.1{-26 Scheduler
        Agenda := \{s_0\};
        While Agenda # Ø
(1)
                 Select some partial schedule s \in Agenda; Agenda := Agenda - \{s\}
                 search for Some s^*(u) \in s;
(2)
                 1 F s^*(u) satisfies R_1 \cup R_2 Then
                         Return s*(u);
                 Else
                         Select constraint c \in R_1 \cup R_2 not satisfied by s^*(u);
(3)
                         Refine s into \{s_i\}, such that each s' \in S_i satisfies c
(4)
                                                        and \bigcup \{s_i\} = s;
                         Perform Constraint Propagation
                 Agenda := Agenda \cup \{S_i\};
```

Figure 2: The basic LR-26 refinement search method.

4.2.5 Performance Tradeoffs

Perhaps the most difficult decisions in constructing the scheduler involve how to flesh out the details of steps 1,2, 3, and 4. The constraint satisfaction and operations research literatures have proposed many heuristic methods for these steps. Unfortunately, due to their heuristic nature, it is not clear what combination of methods best suits this scheduling problem. The power of a heuristic method depends on subtle factors that are difficult to assess in advance. When considering multiple methods, one has to additionally consider interactions between methods.

In LR-26 a key interact ion arises in the tradeoff between the amount of weight vector search vs. refinement search performed by the scheduler (as determined by Step 2). At each step in the refinement search, the scheduler has the opportunity to search in the space of relaxed solutions. Spending more effort in this weight search can reduce the amount of subsequent refinement search. But at some point the savings in reduced refinement search may be overwhelmed by the cost of performing the weight search. This is a classic example of the utility problem [Minton88], and it is difficult to see how best to resolve the tradeoff without intimate knowledge of the form and distribution of scheduling problems.

Another import ant issue for improving scheduling efficiency is the choice of heuristic methods for cent rolling the direct ion of refinement search (as determined by steps 1,3, and 4). Often these methods are stated as general principles (e.g. "first instantiate variables that maximally constrain the rest of the search space" [Dechter92 p. 277]) and there may be many ways to realize them in a particular

scheduler and domain. Furthermore, there are almost certainly interact ions bet ween methods used at different control points that makes it difficult to construct a good ova-all strategy.

These tradeoffs conspire to make manual development and evaluation of heuristics a tedious, uncertain, and time consuming task that requires significant knowledge about the domain and scheduler. In the case of LR-26, its initial control strategy was identified by hand, requiring a significant cycle oft rial-and-error evaluation by the developer over a small number of artificial problems. Even with this effort, the resulting scheduler is still expensive to USC, motivating us to try adaptive techniques.

5 ADAPTIVE PROBLEM SOLVING FOR THE DEEP SPACE NETWORK

We developed an adaptive version of the scheduler, *Adaptive LR-26*, in an attempt to improve its performance. Rather than committing on a particular combination of heuristic strategies, Adaptive LR-26 embodies an adaptive problem solving solution. The scheduler is provided a variety of heuristic methods, and, after a period of adaptation, settles on a particular combination of heuristics that suits the actual distribution of scheduling problems for this domain.

To perform adaptive problem solving, we must formally specify three things: a transformation generator that defines the space of legal heuristic control strategies; a utility function that captures our preferences over strategies in the control grammar; and a representative sample of training problems, Wc describe each of these elements as they relate to the DSN scheduling problem.

5.1 TRANSFORMATION GENERATOR

The description of LR-26 in Figure 2 highlights four points of non-determinism with respect to how the scheduler performs its refinement search. To fully instantiate the scheduler we must specify a way of ordering elements on the agenda, a weight search method, a method for selecting a constraint, and a method for generating a spanning set of refinements that satisfy the constraint. The alternative ways for resolving these four decisions are specified by a *control grammar*, which we now describe. The grammar defines the space of legal search control strategies available to the adaptive problem solver.

S. 1. I Select some partial schedule

The first decision in the refinement search is to choose some partial schedule from the agenda. This selection policy defines the character of the search. Maintaining the agenda as a stack implements depth-first search. Sorting the agenda by some value function implements a best-first search. In Adaptive LR-26 we rest rict the space of methods to variants of depth- first search. Each time a set of refinements is created (Decision 4), they are added to the front of the agenda. Search always proceeds by expanding the first partial schedule on the agenda. Heuristics act by ordering refinements

^{7.} This system has also been referred to by the name of DSN-COMPOSER [Gratch93].

before they are added to the agenda. The grammar specifics several ordering heuristics, sometimes called *value ordering heuristics*, or *look-ahead schemes* in the constraint propagation literature [Dechter92, Mackworth92]. As these methods are entertained during refinement construction, their detailed description is delayed until that section.

Look-ahead schemes decide how to refine partial schedules. Look-back schemes handle the reverse decision of what to do whenever the scheduler encounters a dead end and must backtrack to another partial schedule. Standard depth-first search performs *chronological backtracking*, backing up to the most recent decision. The constraint satisfaction literature has explored several heuristic alternatives to this simple strategy, including backjumping [Gaschnig79], backmarking [Haralick80], dynamic backtracking [Ginsberg93], and dependency-directed backtracking [Stallman77] (see Backer [Baker94] and Frost and Dechter [Frost94] for a recent evaluation of these methods). We are currently investigating look-back schemes for the control grammar but they will not be discussed in this article.

S, 1.2 Search for some relaxed solution

The next dimension of flexibility is in weight-adjusting methods to search the space of possible relaxed solutions for a given partial schedule. The general goal of the weight search is to find a relaxed solution that is closest to the true solution in the sense that as many constraints are satisfied as possible. This can be achieved by minimizing the value of $Z^*(u)$ with respect to u. The most popular method of searching this space is called *subgradient-op timization*[Fisher8 1]. This is a standard optimization method that repeatedly changes the current u in the direction that most decreases $Z^*(u)$. Thus at step i, $u_{i+1} = u_i + i d_i$ where t_i is a step size and d_i is a directional vector in the weight space, The method is expensive but it is guaranteed to converge to the minimum $Z^*(u)$ under certain conditions [Held70]. A less expensive technique, but without the convergence guarantee, is to consider only one weight at a time when finding an improving direction. Thus $u_{i+1} = u_i + t_i d_i$ where is a directional vector with zeroes in all but one location. This method is called *dual-descent*. in both of these methods, weights are adjusted until there is no change in the relaxed solution: $s^*(u_i) = s^*(u_{i+1})$.

While better relaxed solutions will create greater reduction in the amount of subsequent refinement search, it is unclear just where the tradeoff between these two search spaces lies. Perhaps it is unnecessary to spend much time i reproving relaxed schedules. Thus a more radical, and extremely efficient, approach is to settle for the first relaxed solution found. We call this the *first-solution* method. A more moderate approach is to perform careful weight search at the beginning of the refinement search (where there is much to be gained by reducing the subsequent refinement search) and to per-

form the more restricted first-solution search when deeper in the refinement search tree. The *truncated-dual-des cent* method performs dual-descent at the initial refinement search node and then uses the *first-solution* method for the rest of the refinement search

The control grammar includes four basic methods for performing the weight space search:

Weight Search Methods

2a: Subgradient-optimization

2c: '1'runcated-dual-descent

2b: Dual-descent

2d: First-solution

S. 1.3 Select some constraint

If the scheduler cannot find a relaxed solution that solves the original problem, it must break the current partial schedule into a set of refinements and explore them non-deterministically. In Adaptive 1X-26, the task of creating refinements is broken into two decisions: selecting an unsatisfied constraint (Decision 3), and creating refinements that make progress towards satisfying the selected constraint (Decision 4). Lagrangian relaxation simplifies the first decision by identifying a small subset of constraints that appear problematic. However, this still leaves the problem of choosing one constraint in this subset on which to base the subsequent refinement.

The common wisdom in the search community is to choose a constraint that maximally constrains the rest of the search space, the idea being to minimize the size of the subsequent refinement search and to allow rapid pruning if the partial schedule is unsatisfiable. Therefore, our control grammar incorporates several alternative heuristic methods for locally assessing this factor. Given that the common wisdom is only a heuristic, we include a small number of methods that violate this intuition. All of these methods are functions that look at the local constraint graph topology and return a value for each constraint. Constraints can then be ranked by their value and the highest value constraint Chosen. The control grammar implements both a primary and secondary sort for constraints. Constraints that have the same primary value are ordered by their secondary value.

For the sake of simplicity we discuss only measures for constraints belonging to RI. ⁸ Recall that these constraints have the form $\sum a_{ij}v_j \ge b_i$. (The measures are defined analogously for constraints of type R_2 .) We first define measures on time periods. Measures on constraints are functions of the measures of the time periods that participate in the. constraint.

Measures on 'lime Periods

8. This constrainttype suffices to represent the project requirements for the projects implemented in IX-26.

An unforced time period is one that is neither in or out of the schedule (v_i =?). The conflictedness of an unforced t ime period v (with respect to a current partial schedule) is the number of other unforced t ime periods that will be forced out if v is forced into the schedule (because they participate in an antenna constraint with v). If a time period is already forced out of the current partial schedule, it dots not count toward v's conflictedness. Forcing in a time period with high conflictedness will result in many constraint propagations, which reduces the number of ground schedules in the refinement.

The *gain* of an unforced time period v (with respect to a current partial schedule) is the number of unsatisfied project constraints that v participates in. Preferring time periods with high gain will make progress towards satisfying many project constraints simultaneously.

The loss of an unforced time period v (with respect to a current partial schedule) is a combination of gain and conflictedness. Loss is the sum of the gain of each unforced time period that will be forced out if v is forced into the schedule. Time period with high loss are best avoided as they prevent progress towards satisfying many project constraints.

To illustrate these measures, consider the simplified scheduling problem in Figure 3.

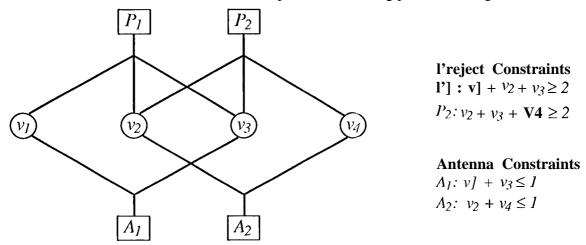


Figure 3: A simplified DSN scheduling problem based on four time periods. There are two project constraints, and two antenna constraints, For example, P_I signifies that at least two of the first three time periods must appear in the schedule, and A_I signifies that either v_I or v_3 may appear in the schedule, but not both. In the solution, only v_2 and v_3 appear in the schedule.

With respect to the initial partial schedule (with none of the time periods forced either in or out) the conflictedness of V_2 is one, because it appears in just one antenna constraint (A_2). If subsequently, V_4 is forced out, then the conflictedness of V_2 drops to zero, as conflictedness is only computed over unforced time periods. The initial gain of V_2 is two, as it appears in both project constraints. Its gain

drops to one if v_3 and V_4 are then forced into the schedule, as P_2 becomes satisfied. The initial loss of V_2 is the sum of the gain of all views conflicting with it (v_4) . The gain of V_4 is one (it appears in P_2) so that the loss of V_2 is one.

Measures on Constraints

Constraint measures (with respect to a partial schedule) can be defined as functions of the measures of the unforced t imc periods that participate in a constraint. The functions max, rein, and total have been defined. Thus, total-conflictedness is the sum of the conflictedness of all unforced time periods mentioned in a constraint, while max-gain is the maximum of the gains of the unforced time periods. Thus, for the constraints defined above, the initial total-conflictedness of P_1 is the conflictedness of V_1 , V_2 and V_3 , V_3 , V_4 and V_5 , V_6 and V_7 , V_8 , and V_8 , V_8 , V_8 , V_8 , V_9 ,

We also define two other constraint measures. The *unforced-periods* of a constraint (with respect to a partial schedule) is simply the number of unforced time periods that are mentioned in the constraint. Preferring a constraint with a small number of unforced time periods restricts the number of refi nements that must be considered, as refinements consider combinations oft i me periods to force into the schedule in order to satisfy the constraint, Thus, the initial unforced-periods of PI is $3(v_1, v_2, and v_3)$.

The *satisfaction-distance* of a constraint (with respect to a partial schedule) is a heuristic measure the number of time periods that must be forced in order to satisfy the constraint. The measure is heuristic because it does not account for the dependencies between time periods imposed by antenna constraints. The initial satisfaction-distance of P_1 is two because two time periods must be forced in before the constraint can be satisfied,

Given these constraint measures, constraints can be ordered by some. measure of their worth. To complete the definition of a constraint ordering heuristic we must specify if a measure is to be preferred or penalized. For example we may prefer constraints with high total conflictedness. This heurist ic is denoted as *prefer-total-conflictedness*. Not al I possible combinat ions seem meaningful so the control grammar for Adaptive LR-26 implements the following nine constraint ordering heuristics:

Constraint Selection Methods

3a: Prefer-max-gai n3f: Penalize-total-conflictedness3b: Prefer-total-gain3g: Prefer-min-conflicteclness

3c: Penalize-max-loss 3h: Penali~,c-unforced-periods

3d: Penalize-max-conflictedness 3i: Penali~,c-satisfaction-distance

3e: Prefer-total-conflictcdness

5.1.4 Refine partial schedule

Given a selected constraint, the scheduler must create a set of refinements that make progress towards satisfying the constraint. If the constraint is a member of $R_I(\Sigma a_{ij}v_j \ge b_i)$ then some time periods on the left-hand-side must be forced into the schedule if the constraint is to be satisfied, Thus, refinements are constructed by identifying a set of ways to force time periods in or out of the partial schedules such that the refinements form a spanning set: $\bigcup \{s_i\}$ =s. These refinements are then ordered and added to the agenda. Again, for simplicity we restrict discussion to constraints in R_I .

The Basic Refinement Method

The basic method for refining a partial schedule is to take each unforced time period mentioned in the constraint and create a refinement with the time period v_j forced into the schedule. Thus, for the constraints defined above, there would be three refinements to constraint P1, one with v_1 forced IN: one with v_3 forced IN, and one with v_3 forced IN.

Each refinement is further refined by performing constraint propagation (arc consistency) to determine some local consequences of this new restriction. Thus, every time period that conflicts with v_j is forced out of the refined partial schedule, which in turn may force Other time periods to be included, and so forth. By this process, some refinements maybe recognized as inconsistent (contain no ground solutions) and arc pruned from the search space (for efficiency, constraint propagation is only performed when partial schedules arc removed from the agend a).

Once the set of refinements has been created, they are ordered by a value ordering heuristic before being placed on the agenda. As with constraint ordering heuristics, there is a common wisdom for creating value ordering heuristics: prefer refinements that maximized the number of future options available for future assignments [Dechter87, Haralick80]. The control grammar implements several heuristic methods using measures on the time periods that created the refinement. For example, one way to keep options available is to prefer forcing in a time period with minimal conflictedness. As the common wisdom is only heuristic, we also incorporate a method that violates it. The control

grammar includes the following value ordering heuristics that are derived from the measures on time periods:

Value Ordering Methods

1a: Prefer-gain 1d: Prefer-conflictedness

1 b: Penalize-Joss 1 c: Arbitrary

1 c: Penalize-conflictcdncss

where the last method, arbitrary, just uses the ordering of the time periods as they appear in the constraint.

The Systematic Refinement Method

The basic refinement method has one unfortunate property that may limit its effectiveness. The search result ing from this refinement method is *unsystematic* in the sense of McAllister and Rosenblitt [McAllester91]. This means that there is some redundancy in set of refinements: $s_j \cap s_j \neq \emptyset$. Unsystematic search is inefficient in that the total size of the refinement search space will be greater than if a systematic (non-redundant) refinement method is used. This may or may not be a disadvantage in practice as scheduling complexity is driven by the size of the search space actually explored (the *effective search space*) rather than its total size. Nevertheless, there is good reason to suspect that a systematic method will lead to smaller effective search spaces,

A systematic refinement method chooses a time period that helps satisfy the selected constraint and then forms a spanning set of two refinements: one with the time period forced in and one with the time period forced out. These refinements are guaranteed to be non-overlapping. The systematic method incorporated in the control grammar uses the value ordering heuristic to choose which unforced time period to use. The two refinements are ordered based on which makes immediate progress towards satisfying the constraint (e.g., v=IN is first for constraints in R_I). The control grammar includes both the basic and systematic refinement methods:

Refinement Methods

4a: Basic-Refinement

4b: Systematic-Refinement

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For the problem specified in Figure 3, when systematically refining constraint PI, one would use the value ordering method to select among views VI, V₂, and v₃. If V₂ were selected, two refinements would be proposed, one with V₂ forced IN and one with V₃ forced OUT.

```
CONTROL. STRATEGY := VALUE ORDERING A

WEIGHT SEARCHMETHOD A

PRIMARY CONSTRAINT ORDERING A

SECONDARY CONSTRAINT ORDERING A

REFINEMENT METHOD
```

```
VALUE ORDERING := {la, lb, 1c,1d,1e}

WEIGHT SEARCH MIIT 110D := {2a, 2b, 2c, 2d}

PRIMARY CONSTRAINT ORDERING := {3a, 3b, 3c, 3d, 3c, 3f, 3g, 3h, 3i}

SECONDARY CONSTRAINT ORDERING := {3a, 3b, 3c, 3d, 3e, 3f, 3g, 3h, 3i}

REFINEMENT METHOD := {4a, 4b}
```

Figure 4: Control grammar for Adaptive LR-26

The control grammar is summarized in Figure 4. The original expert cent rol strategy developed for LR-26 is a particular point in the control space defined by the grammar: the value ordering method is arbitrary (1c); the weight search is by dual-descent(2b); the primary constraint ordering is penalize-unforced-periods (3h); there is no secondary constraint ordering, thus this is the same as the primary ordering; and the basic refinement method is used (4a).

S. 1.5 Meta-control Knowledge

The constraint grammar defines a space of close to three thousand possible control strategies. The quality of a strategy must be assessed with respect 10 a distribution of problems, therefore it is prohibitively expensive to exhaustively explore the control space: taking a significant number of examples (say fifty) on each of the strategies at a cost of 5 CPU minutes per problem would require approximately 450 CPU days of effort.

COMPOSER requires a transformation generator to specify alternative strategies. These strategies are explored via hillclimbing search. In this case, the obvious way to proceed is to consider all single method changes to a given control strategy. However the cost of searching the strategy space and quality of the final solution depend to a large extent on how hillclimbing proceeds, and the obvious way need not be the best. In Adaptive 1X-26, we augment the control grammar with some domain-specific knowledge to help organize the search. Such knowledge includes, for example, our prior expectation that certain control decisions would interact, and the likely importance of the different control decisions. The intent of this "recta-control knowledge" is to reduce the branching factor in the control strategy search and improve the expected utility of the locally optimal solution found.

This approach led to a layered search through the strategy space. Each control decision is assigned to a level. The control grammar is search by evaluating all combinations of methods at a single level, adopting the best combinations, and then moving onto the next level. The organization is shown below:

Level 0: {weight search method }
Level 1: {Refinement method}

Level 2: {Secondary constraint ordering, Value ordering}

Level 3: {Primary constraint ordering }

The weight search and refinement control points are separate, as they seem relatively independent from the other control points, in terms of their effect on the overall strategy. While there is clearly *some* interaction between weight search, refinement construction, and the other control points, a good selection of methods for pricing and alternative construction should perform well across all ordering heurist its. The primary constraint ordering met hod is relegated to the last level because some effort was made in optimizing this decision in the expert strategy for LR-26, and we believed that it was unlikely the default strategy could be improved.

Given this transformation generator, Adaptive LR-26 performs hillclimbing across these levels. It first entertains weight adjustment methods, then alternative construction methods, then combinations of secondary constraint sort and child sort methods, and finally primary constraint sort methods. Each choice is made given the previously adopted methods.

This layered search can be viewed as the consequence of asserting certain t ypcs of relations between control points. independence *relations* indicate cases in which the utility of methods for one control point is rough] y independent of the methods used at other control points. *Dominance relations* indicate that the changes in utility from changing methods for one control point are much larger than the changes in utility for another control point, Finally, inconsistency relations indicate when a method M_1 for control point X is inconsistent with method M_2 for control point Y. This means that any strategy using these methods for these control points need not be considered.

S.2 EXPECTED UTILITY

As previously mentioned, a chief design requirement for LR-26 is that the scheduler produce solutions (or prove that none exist) efficiently. This behavioral preference can be expressed by a utility function related to the computational effort required to solve a problem. As the effort to produce a schedule increases, the utility of the scheduler on that problem should decrease. In this paper, we characterize this preference by defining utility as the negative of the CPU time required by the scheduler on a problem. Thus, Adaptive LR-26 tunes itself to strategies that minimize the average time

to generate a schedule (or prove that one dots not exist). Other utility functions could be entertained. in fact, more recent research has focused on measures of schedule quality (see [Chien94] for some preliminary results on this direction),

5.3 PROBLEM DISTRI HUTION

Adaptive LR-26 needs a representative sample of training examples for its adaptation phase. Unfortunately, DSN Operations has only recently begun to maintain a database of scheduling problems in a machine readable format. While this will ultimately allow the scheduler to tune itself to the actual problem distribution, only a small body of actual problems was available at the time of this evaluation. Therefore, we resorted to other means to create a reasonable problem distribution.

We constructed an augmented set of training problems by syntactic manipulation of the set of real problems. Recall that each scheduling problem is composed oft wo components: a set of project requirements, and a set of time periods. Only the time periods change across scheduling problems, so we can organize the real problems into a set of tuples, one for each project, containing the weekly blocks of time periods associated with it (one entry for each week the project is scheduled). The set of augmented scheduling problems is constructed by taking the cross product of these tuples. Thus, a weekly scheduling problem is defined by combining one weeks worth of time periods from each project (time periods for different projects may be drawn from different weeks), as well as the project requirements for each. This simple procedure defines set of 6600 potential scheduling problems.

Two concerns led us to use only a subset of these augmented problems. First, a significant percentage of augmented problems appeared much harder to solve (or prove unsatisfiable) than any of the real problems (on almost half of the constructed problems the scheduler d id not terminate, even with large resource bounds). That such "hard" problems exist is not unexpected as scheduling is NP-hard, however, their frequency in the augmented sample, seems d isproportionately high. Second, the existence of these hard problems raises a secondary issue of how best to terminate search. The standard approach is to impose some arbitrary resource bound and to declare a problem unsatisfiable if no solution is found within this bound. Unfortunately this raises the issue of what sized bound is most reasonable. We could have resolved this by adding the resource bound to the control grammar, however, at this point in the project we settled for a simpler approach. Instead, we address this and the previous concern by excluding from the augmented problem distribution those problems that seem "fundamentally intractable." What this means in practice is that we exclude problems that could not be solved by any of a large set of heuristic methods within a five minute resource bound. (For a discussion of how we arrived at this CPU bound see Appendix A.) This results in a reduced set of about three thousand scheduling problems. For comparative purposes, and to show the generality of adap-

tive problem solving, we include a secondary set of evaluations based on all 6600 augmented problems.

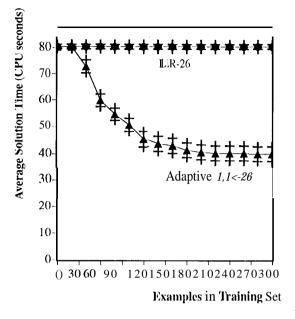
6 EMPIRICAL EVALUATION

The statistical theory that underlies COMPOSER predicts that, with high probability, Adaptive LR-26 will improve scheduling performance over the distribution of problems. This can be seen as two basic claims that can be tested empirically. First, Adaptive LR-26 should identify transformations that improve the initial expert strategy associated with LR-26. Second, it should identify these transformations with the confidence predicted by the statistical theory. We are also claiming that, at least in practice COMPOSER can go beyond simply improving performance, and identify strategies that rank highly when judged with respect to the whole space of possible strategies. A third claim, therefore, is that Adaptive LR-26 will find better strategies than if we simply picked the best of a large number of randomly selected strategies. Besides testing these three claims, we are also interested in three secondary questions: how quickly does the technique improves expected utility (e.g., how many examples are required to make statistical inferences?); can Adaptive LR-26 improve the number problems solved (or proved unsatisfiable) within the resource bound; and how sensitive is the effectiveness of adaptive problem solving to changes in the distribution of problems.

6.1 METHODOLOGY

Our evaluation is influenced by the stochastic nature of adaptive problem solving. During adaptation, Adaptive LR-26 is guided by a random selection of training examples according to the problem distribution. As a result of this random factor, the system will exhibit different behavior on different runs of the system. On some runs the system may learn high utility strategies; on other runs the randoJn examples may poorly represent the distribution and the system may adopt transformations with negative utility. Thus, our evaluation is directed at assessing the *expected* performance of the adaptive scheduler by averaging results over twenty experimental trials.

For these experiments, the scheduler is allowed to adapt to 300 scheduling problems drawn randomly from the problem distribution described above. The expected utility of all learned strategies is assessed on an independent test set of 1000 test examples drawn randomly from the complete set of three thousand. The adapt at ion rate is assessed by recording the strategy learned by Adaptive LR-26 after every 20 examples. Thus we can see the result of learning with only twenty examples, only fort y examples, etc. We measure the statistical error of the technique (the probability of adopting a transforJnation with negative incremental utility) by performing eighty runs of the system on eighty distinct training sets drawn randomly from the problem distribution. We measure the distributional sensitivity of the technique by evaluating the adaptive scheduler on a second distribution of



Summary of Results			Dist. 1
Avg. Solution Time seconds ter prob.	LR-26		80
	Adaptive LR-26	avg. across trials	40
		best strategy	24
		worst strategy	55
Statistical Error Rate		predicted	5%
		observed	3%
ate cobs.		LR-26	79%
Solution Rate % of solvable probs	Adaptiwe LR-26	avg. across trials	95%
		best strategy	97%
		worst strategy	86%

Figure 5. Learning curve showing performance as a function of the number of training examples and table of experimental results.

problems. Recall that we purposely excluded inherently difficult scheduling problems from the augmented set of problems. If added, these excluded problems should make adaptation more difficult as no strategy is likely to provide a noticeable improvement within the five minute resource bound. The second evaluation includes these difficult problems

A third evaluation assesses the relative quality of the strategies identified by Adaptive LR-26 when compared with other strategies in the strategy space. This is inferred by comparing the expected utility of the learned strategies with several strategies drawn randomly from the space. This also provides an opportunity to assess the quality of the expert strategy, and thus give a sense of how challenging it is to improve it.

COMPOSER, the statistical component of the adaptive scheduler, has two parameters that govern its behavior. The parameter δ specifics the acceptable level of statistical error (this is the chance that the technique will adopt a bad transformation or reject a good one). In Adaptive LR-26, this is set to a standard value of 5%. COMPOSER bases each statistical inferences on a minimum of n_0 examples. in Adaptive LR-26, n_0 is set to the empirically determined value of fifteen.

6.2 OVERALL RESULTS — DSN DISTRI BUTION

Figure 5 summarizes the results of adaptive problem solving over the constructed DSN problem distribution. The results support the t wo primary claims. First, the system learned search control strategies that yielded a significant improvement in performance. Adaptive problem solving reduced the

average time to solve a problem (or prove it unsatisfiable) from 80 to 40 seconds (a 50% improvement). Second, the observed statistical error fell well within the predicted bound, Of the 370 transformations adopted across the twenty trials, only 3% decreased expected utility.

Due to the stochastic nature of the adaptive scheduler, different strategies were learned on different trials. All learned strategies produced at least some improvement in performance, The best of these strategies required only 24 seconds on average to solve a problem (an improvement of 70%). The fastest adaptations occurred early in the adaptation phase and performance improvements decreased steadily throughout. It took an average of 62 examples to adopt each transformation. Adaptive LR-26 showed some improvement over the non-adaptive scheduler in terms of the number of problems that could be solved (or proven unsatisfiable) within the resource bound. LR-26 was unable to solve21% of the scheduling problems within the resource bound. One adaptive strategy reduced this substantially reduced this number to 3%.

An analysis of the learned strategies is revealing. Most of the performance improvement (about one half) can be traced to modifications in LR-26's weight search method. The rest of the improvements arc divided equally among changes to the heuristics for value ordering, constraint selection, and refinement. As expected, changes to the primary constraint ordering only degraded performance. The top three strategies arc illustrated in Figure 6.

1) Value ordering: penalize-conflictedness (1 c)

Weight search: first-solution (2d)

Primary constraint ordering: penalize-unforced-periods (3h)
Secondary constraint ordering: prefer-total-conflictc(incss (3e)
Refinement method: systematic-refinement (4b)

2) Value ordering: prefer-gain (1a)
Weight search: first-solution (2d)

Primary constraint ordering: penalize.-unforced-periods (3h)
Secondary constraint ordering: prefer-total-conflictedness (3e)
Refinement method: system:i[ic-refinement (4b)

3 Value ordering: penalize-conflictedness (1 c)

Weight search: first-solution (2d)

Primary constraint ordering: penalize-unforced-pcrio(is (3h) Secondary constraint ordering: penalize-satisfaction-distance (3i)

Refinement method: systematic-refinement (4b)

Figure 6: The three highest utility strategies learned by Adaptive LR-26.

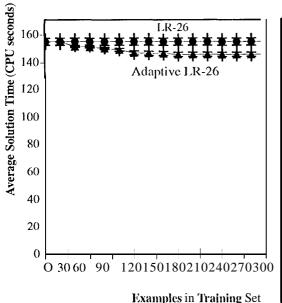
For the weight search, all of the learned strategies used the first-solution method (2d). It seems that, at least in this domain and problem distribution, the reduction in refinement search space that results from better relaxed solutions is more than offset by the additional cost of the weight search. The scheduler did, however, benefit from the reduction in size that results from a systematic refinement method.

More interestingly, Adaptive LR-26 seems to have "rediscovered" the common wisdom in heuristic constraint-satisfaction search. When exploring new refinements, it is often suggested to chose the least constrained value of the most constrained constraint. The best learned strategies follow this advice while the worst strategies violate it, In the best strategy, the time period with lowest conflictedness is least constraining (in the sense that it will tend to produce. the least constraint propagations) and thus produces the least commitments on the resulting partial schedule. By this same argument, the constraint with the highest total conflicted will tend to be the hardest to satisfy.

6.3 OVERALL RESULTS — FULL AUGMENTED DISTRIBUTION

Figure 7 summarizes the results for the augmented distribution. As expected, this distribution proved more challenging for adaptive problem solving. Nevertheless, modest performance improvements were still possible, lending support to our claimed generality of the adaptive problem solving approach. Learned strategies reduced the average solution time from 156 to 146 seconds (an 6% improvement). The best learned strategies required 133 seconds on average to solve a problem (an improvement of 15%). The observed statistical accuracy did not significantly differ from the theoretically predicted bound, although it was slightly higher than expected: of 397 transformations were adopted across the trials, 6% produced a decrease in expected utility. The introduction of the difficult problems resulted in higher variance in the distribution of incremental utility values and this is reflected in a higher sample complexity: an average of 118 examples to adopt each transformation. Some improvement was noted on the supposedly int ractable problems. One strategy learned by Adaptive LR-26 increased the number of problems that could be processed within the resource bound 51\$10 to 57%.

Onc interesting result of this evaluation is that, unlike the previous evaluation, the best learned strategies use truncated-dual-descent as their weight search method (the strategies were similar along other control dimensions). 'I'his illustrates how even modest changes to the distribution of problems can influence the design tradeoffs associated with a problem solver: in this case, changing the tradeoff between weight and refinement search.



Summary of Results			Dist. 1-
Avg. Solution Time seconds per prob.	LR-26		156
	Adaptive 1>R-26	avg. across trials	146
		best strategy	133
		worst strategy	150
Statistical Error Rate		predicted	5%
		obscrved	6%
a te robs.	1.1{-26		5190
Solution Rate % of solvable probs.	Adaptive LR-26	avg. across trials	54%
		best strategy	57%
		worst strategy	51%

Figure 7. Learning curves and table of experimental results showing performance over the augmented distribution (including "intractable" problems).

6.4 QUALITY OF LEARNED STRATEGIES

The third claim is that, in practice, COMPOSER can identify strategies that rank highly when judged with respect to the whole strategy space. A secondary question is how well does the expert strategy perform. The improvements of Adaptive LR-26 are of little significance if it the expert strategy performs worse than most strategies in the space. Alternatively, if the expert strategy is extremely good, its improvement is compel 1 ing.

As a way of assessing these claims we estimate the probability of selecting a high utility strategy given that we c1100sc it randomly from one of three strategy spaces: the space of all possible strategies (expressible in the transformation grammar), the space of strategies produced by Adaptive 1.1<-26, and the trivial space cent aining only the expert strategy. This corresponds to the problem of estimating a *probability density function* (p.d.f.) for each space: a p.d.f., f(x), associated with a random variable gives the probability that an instance of the variable has value x. More specifically we want to estimate the density functions, $f_s(u)$, which is the probability of randomly selecting a a strategy from space s that has expected utility u.

We use a non-parametric density estimation technique called the kernel method to estimate $f_s(u)$ (as in [93]). To estimate the density function of the whole space, we randomly selected and tested thirty strategies. All of the learned strategies are used to estimate the density of the learned space. (In both cases, five percent of the data was withheld to estimate the bandwidth parameter used by the kernel

method.) The p.d.f. associated with the single expert strategy is estimated using a normal model fit to the 1000 test examples from the previous evaluation.

6.4.1 DSN Distribution

Figure 8 illustrates the results for the DSN distribution. In this evaluation the learned strategies significantly outperformed the randomly selected strategies. Thus, one would have to select and test many strategies a random before finding one of comparable expected utility to one found by Adaptive LR-26. The results also indicate that the expert strategy is already a good strategy (as indicated by the relative positions of the peaks for the expert and random strategy distributions), indicating that the improvement due to Adaptive LR-26 is significant and non-trivial.

The results provide additional insight into Adaptive LR-26's learning behavior. That the p.d.f for the learned strategies contains several peaks, graphically illustrates that different local maxima exist for this problem. Thus, there may be benefit in running the system multiple times and choosing the best strat 3y. It also suggests that techniques designed to avoid local maxima would be beneficial.

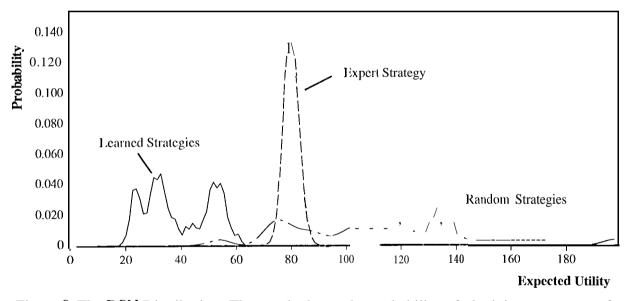


Figure 8: The DSN Distribution. The graph shows the probability of obtaining a strategy of a particular utility, given that it is chosen from (1) the set of all strategies, (2) the set of learned strategies, or (3) the expert strategy.

6.4.2 Full Augmented Distribution

Figure 9 illustrates the results for the full augmented distribution. The results are similar to the DSN distribution: the learned strategies strategies again outperformed the expert strategy which in turn again outperformed the randomly selected strategies. The data shows that the expert strategy is significantly better than randomly selected strategies. Together, these two evaluations support the claim that Adaptive LR-26 is selecting high performance strategies. Even though the expert strategy

is quite good when compared with the complete strategy space, the adaptive algorithm is able to improve the expected problem solving performance.

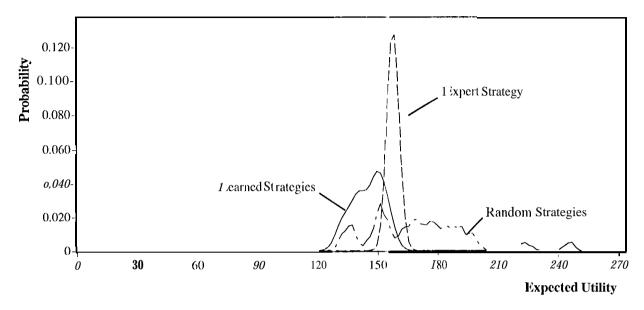


Figure 9: The Full augmented distribution. The graph shows the probability of obtaining a strategy of a particular utility, given that it is chosen from (1) the set of all strategies, (2) the set of learned strategies, or (3) the expert strategy.

7 FUTURE WORK

The results of applying an adaptive approach to deep space network scheduling are very promising. We hope to build on this success in a number of ways. We discuss these directions as they relate to the three basic approaches to adaptive problem solving: syntactic, generative, and statistical.

7.1 SYNTACTIC APPROACHES

Syntactic approaches attempt to identify control strategies by analyzing the structure of the domain and problem solver. In 1.1<-26, our use of recta-control knowledge can be seen as a syntactic approach; although unlike most syntactic approaches that attempt to identify a specific combination of heuristic methods, the recta-knowledge (dominance and indifference relations) acts as constraints that only partially determine a strat egy. An advantage of this weakening of the syntactic approach is that it lends itself to a natural and complementary interaction with statistical approaches: structural information restricts the space of reasonable strategies, which is then explored by statistical techniques. An important question concerning such knowledge is to what extent does it contribute to the success of our evaluations, and, more interestingly, how could such information be derived automatically from a structural analysis of the domain and problem solver. We are currently performing a series of experiments to address the former question. A step towards the resolving the second questions.

lion would be to evaluate in the context of LR-26 some of the structural relationships suggested by recent work in this area [Frost94, Stone94].

7.2 GENERATIVE APPROACHES

Adaptive LR-26 uses a non-generative approach to conjecturing heuristics. Our experience in the scheduling domain indicates that the performance of adaptive problem solving is inextricably tied to the transformations it is given and the expense of processing examples. Just as an inductive learning technique relics on good attributes, if COMPOSER is to be effective, there must exist good methods for the control points that make up a strategy. Generative approaches could improve the effectiveness of Adaptive LR-26. Generative approaches dynamically construct heuristic methods in response to observed problem-solving inefficiencies. The advantage of waiting until inefficiencies are observed is twofold. First, the exploration of the strategy space can be much more focused by only conjecturing heuristics relevant to the observed complications. Second, the conjectured heuristics can be tailored much more specifically to the characteristics of these observed complications.

Our previous app] i cat ion of COMPOSER achieved greater performance improvements that Adaptive LR-26, in part because it exploited a generative technique to construct heuristics [Gratch92]. Ongoing research is directed towards incorporating generative methods into Adaptive LR-26. Some preliminary work analyzes problem-solving traces to induce good heuristic methods. The constraint and value ordering metrics discussed in Section 5.1.3 are used to characterize each search node. This information is then fed to a (iccision-tree algorithm, which tries to induce effective heuristic methods. These generated methods can then be evaluated statistically.

7.3 STATISTICAL APPROACHES

Finally there arc directions of future work devoted towards enhancing the power of the basic statistical approach, both for Adapt ive LR-26 in particular, and for statist ical approaches in general. For the scheduler, there arc two important considerations: enhancing the control grammar and exploring a wider class of utility functions, Several methods could be added to the control grammar. For example, an informal analysis of the empirical evaluations suggests that the scheduler could benefit from a look-back scheme such as back jumping [Gaschnig79] or backmarking [Haralick80]. We would also like to investigate the adaptive problem solving methodology on a richer variety of scheduling approaches, besides integer programming. Among these would be more powerful bottleneck centered techniques [Bicfeld89], constraint-based techniques [Smith93], opportunistic techniques [Sadch94], reactive techniques [Smith94] and more powerful backtracking techniques such as [Xiong92].

The current evaluation of the scheduler focused on problem solving time as a utility metric, but future work will consider how to improve other aspects of the schedulers capabilities. For example, by choosing another utility function we could guide Adaptive LR-26 towards influencing other aspects of LR-26's behavior such as: increasing the amount of flexibility in the generated schedules, increasing the robustness of generated schedules, maximizing the number of satisfied project constraints or reducing the implementation cost of generated schedules. These alternative utility functions are of great significance in that they provide much greater leverage in impacting actual operations. For example, finding heuristics which will reduce DSN schedule implementation costs by 3% has a much greater impact than reducing the automated scheduler response time by 3%. Some preliminary work has focused on improving schedule quality [Chien94].

More generally, there are several ways to improve the statistical approach embodied by COMPOS-ER. Statistical approaches involve two processes, estimating the utility of transformations and exploring the space of strategies. The process of estimating expected utilities can be enhanced by more efficient statistical methods [Chien95, Moore94, Nelson95], alternative statistical decision requirements [Chien95] and more complex statistical models that weaken the assumption of normality [Smyth92]. The process of exploring the strategy space can be improved both in terms of its efficiency and susceptibility to local maxima, Moore and Lee propose a method called *schemata search* to help reduce the combinatorics of the search. Problems with local maxima can be mitigated, albeit expensively, by considering all k-wise combinations of heuristics (as in MULTI-TAC[Minton93] or level 2 of Adaptive LR-26's search), or by standard numerical optimization approaches such as repeating the hillclimbing search several times from different start points.

One final issue is the expense in processing training examples. In the LR-26 domain this cost grows linearly with the number of candidates at each hillclimbing step. While this is not bad from a complexit y standpoint, it is a pragmatic concern. There have been a few proposals to reduce the expense in gathering statistics. in [Gratch92] we exploited properties of the transformations to gather statistics from a single solution attempt. That system required that the heuristic methods only act by pruning refinements that are guaranteed unsatisfiable. Greiner and Jurisica [Greiner92] discuss a similar technique that eliminates this restriction by providing upper and lower bounds on the incremental utility oft ransformat ions. Unfortunate] y, neither of these approaches could be applied to LR-26 so devising methods to reduce the processing cost is an important direction for future work.

^{&#}x27;9. For a description of preliminary work in this area see [Chien94].

8 CONCLUSIONS

Although many scheduling problems are intractable, for actual sets of constraints and problem distributions, heuristic solutions can provide acceptable performance. A frequent difficulty is that determining appropriate heuristic methods for a given problem class and distribution is a challenging process that draws upon deep knowledge of the domain and the problem solver used. Furthermore, if the problem distribution changes sometime in the future, one must manually re-evaluate the effectiveness of the heuristics.

Adaptive problem solving is a general approach for reducing this developmental burden. This paper has described the application of adaptive problem solving, using the LR–26 scheduling system and the COMPOSER machine learning system, to automatically learn effective scheduling heuristics for Deep Space Network communications scheduling. By demonstrating the application of these techniques to a real-world application problem, this paper has makes several contributions. First, it provides an example of how a wide range of heuristics can be integrated into a flexible problem-solving architecture — providing an adaptive problem-solving system with a rich control space to search. Second, it demonstrates that the difficulties of local maxima and large search spaces entailed by the rich control space can be tractably explored. Third, the successful application of the COMPOSER statistical techniques demonstrates the real-world applicability of the statistical assumptions underlying the COMPOSER approach. Fourth, and most significantly, this paper demonstrates the viability of adaptive problem solving. The strategies learned by the adaptive problem solving significantly out performed the best human expert derived solution.

APPENDIX A: DETERMINATION OF THE RESOURCE BOUND

A good CPU bound to characterize "intractable" problems should have the characteristic that increasing the bound s11ouIcI have little effect on the proportion of problems solvable. In order to determine the resource bound to define "intractable" DSN scheduling problems we empirically evaluated how likely 1.1<–26 was to be able to solve a problem with various resource bounds. informally, we experimented to find a bound of 5 CPU minutes. We then formally verified this bound by taking those problems not solvable within the resource bound of 5 CPU minutes, allowing LR–26 an additional CPU hour to attempt to solve the problem, and observing how this affected solution rate. As expected, even allocating significant more CPU time, LR-26 was not able to solve many more problems. Figure 10 below shows the cumulative percentage of problems solved; from those not solvable within the 5 minute CPU bound. This curve shows that even with another CPU hour (per problem!), only about 12% of the problems became solvable. This graph also shows the 95% confidence intervals for this cumulative curve. In light of these results, the fact that one learned strategy was able

to increase by 1 8% the percentage of problems solvable within the resource bound is even more impressive. In effect, learning this strategy has a greater impact than allocating another CPU hour per problem.

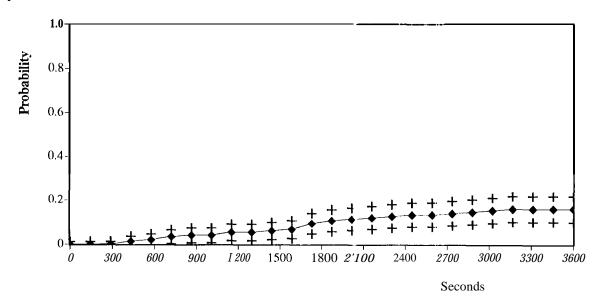


Figure 10: Given that a problem cannot be solved in five minutes, show the probability that it can be solved in up to an hour more time (with 95% confidence intervals).

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